Computer-Aided Measurement of Solid Breast Tumor Features on Ultrasound Images

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Abstract. This paper presents a new approach in the application of computer vision techniques to the diagnosis of solid breast tumors on ultrasound images. Most works related to medical image analysis for breast cancer detection refer to mammography. However, radiologists have proved the significance of some aspects observed on ultrasound images, among which are spiculation, calcifications, ellipsoid shape, dimensions, echogenicity, capsule, angular margins, lobulations, shadowing and ramifications. We have developed a common framework for the analysis of these criteria, so that a series of parameters are available for the physicians to decide whether the biopsy is necessary or not. We present a set of mathematical methods to extract objective evidence of the presence or absence of the diagnostic criteria. This system is able to extract the relevant features for solid breast nodules with high accuracy and represents a very valuable help in the assessment of radiologists.

1 Introduction

There are certain criteria which are used by the physicians to determine whether a solid breast nodule is benign or malignant. This work uses the computational techniques for the study and classification of shapes and textures to help the physicians in the early diagnosis of breast tumors on ultrasound images. Contrary to other works which deal with mammographies, this one is based on the analysis of ultrasound images, in which a series of diagnostic factors can be observed. Some previous works try to adjust the parameters of the ultrasound systems to help in the decision making process [1], segment the tissues [2], or deal with certain particular aspects of the nodules, such as texture [3] or general shape [4]. The analysis of ultrasound images that we propose allows performing precise measurements of a series of diagnostic factors in order to characterize each nodule according to the values of the parameters which have been obtained.

Spiculation, taller than wide shape, angular margins, markedly hypoechoic appearance, acoustic shadowing, calcifications, ramifications and microlobulations are considered as malignant findings which lead the physicians to carry

Fig. 1. Markedly hypoechoic nodule (left) and hyperechoic nodule (right)

out a biopsy. On the other hand, hyperechogenicity, ellipsoid shape, two or three gentle lobulations as well as a thin and echogenic capsule suggest the benignity of the nodule [5].

It is not always easy for a human observer to measure some of these features and provide objective evidence of the benignity or malignancy of the tumor. However, computer vision techniques may help detecting some of them and supplying numerical measurements of the presence and relevance of these factors, in such a way that the risk of overlooking a malignant nodule can be reduced [6] [7]. The purpose of this work is not the substitution of the human observer or the physician's interpretation, but the addition of a precise, objective and invariant examiner which can draw the specialist's attention to those areas where each diagnostic factor is likely to be present.

2 Description of the Diagnostic Criteria

In this section, we will describe each one of the criteria that will be considered in the diagnosis of the nodules, both malignant and benign. These criteria have been extracted and adapted from [5]. We will also present some examples of the results provided by the computer-aided system.

First, we will consider the generation of echo by the nodule and the area around it. The hyper or hypoechogenicity of a nodule, i.e. the excessive or defective generation of echoes by that nodule, is measured with respect to the echogenicity of the fat of that particular woman, since it is the relative intensity and not the absolute one that determines whether it is hyper or hypo-echoic. This feature is considered because of the hyperechogenicity of some benign tumors and the marked hypoechogenicity of malignant nodules. In fact, the central part of two-thirds of malignant solid breast nodules is very hypoechoic with respect to fat. In Fig. 1, we can see an example of a markedly hypoechoic nodule (left) and a hyperechoic nodule (right).

Not only the generation of echo within the nodule is relevant, but also how the region under it is affected. A nodule is said to produce acoustic shadow if the ultrasound is attenuated when crossing through it. In this case, the region

Fig. 2. Nodule without acoustic shadowing (left) and with acoustic shadowing (right)

Fig. 3. Wider-than-tall nodule (left) and taller-than-wide nodule (right)

beyond the nodule, from the point of view of the ultrasound emitting device, is darker than the region at the same level which is not under the nodule, since its emission of echo is not altered by the nodule's being in between. In Fig. 2, we observe how a nodule can leave the generation of echo unaltered (left) or interfere it (right). The generation of shadowing is considered as a malignant factor.

We will now focus on the general shape of the nodule. A nodule is said to be taller than wide when it is greater in the direction normal to the skin than in the parallel ones. When this ratio is quite high, the possibility of being analyzing a malignant nodule increases, since this reflects that the nodule is growing across normal tissue planes. On the other hand, benign nodules usually affect a single tissue and appear perpendicular to the direction of the ultrasound signals. Figure 3 shows a wider-than-tall nodule (left) and a taller-than-wide one (right).

An ellipsoid shape increases the probability of the nodule's being benign, and even if a nodule does not present an ellipsoid-like shape, it is considered as benign if it presents two or three smooth, well circumscribed and gentle lobulations. Figures 4 and 5 present a nodule with elliptical shape and a nodule with two smooth and gentle lobulations, respectively, as well as the ellipses extracted by the computer-aided system to help classifying the nodules.

Fig. 4. Ultrasound image of a solid breast nodule (left), contour and ellipse extracted from that contour (right)

Fig. 5. Ultrasound image of a solid breast nodule (left), contour and combination of two ellipses extracted from that contour (right)

Contrary to the elliptical shapes described above, malignant breast nodules may present projections from the surface of the nodule which extend radially within a duct towards the nipple (duct extension) and/or within ducts away from the nipple (branch pattern). Figure 6 shows a nodule with ramifications, which have been signaled by the system.

Some other factors do not refer to the general shape, but to local variations of the contour. For example, the finding of angular margins makes the nodule suspicious of being malignant. Angular margins refer to the contour of the junction between the hypoechoic or isoechoic solid nodule and the surrounding tissues. The entire surface of the lesion must be surveyed, since they may involve only a part of it. Similarly, microlobulations are observed as small ellipsoid arcs in certain regions of the contour and are frequently associated with angular margins. Figures 7 and 8 show the angular margins and microlobulations extracted for a nodule, respectively.

Spiculation consists of contrasting lines radiating out perpendicularly from the surface of the nodule. Figure 9 shows the spiculated areas extracted for a nodule.

Fig. 6. Ultrasound image of a solid breast nodule (left), contour and ramifications extracted by the system (right)

Fig. 7. Ultrasound image of a solid breast nodule (left), contour and angular margins extracted from that contour (right)

Finally, the presence of echogenic calcifications within a solid breast nodule is worrisome for malignancy. Calcifications are identified as highly contrasting white points inside the nodule. Figure 10 shows an example of a nodule with calcifications and where they are located by the computer.

In the following section, we show how the ultrasound images have been processed to analyze these factors on them.

3 Computer Processing of the Diagnostic Criteria

In this section, we will show how the criteria described above have been processed by the computer-aided system. First, we will explain how the nodule has been segmented, then we will present the processing of the intensity-related criteria, and finally we will explain how the shape of the nodule has been analyzed.

3.1 Image Segmentation

Before measuring the diagnosis criteria on the nodule, it must be located and delimited. Thus, we must segment the interesting area and the background in

Fig. 8. Ultrasound image of a solid breast nodule (left), contour and microlobulations extracted from that contour (right)

Fig. 9. Ultrasound image of a solid breast nodule (left), contour and spiculations extracted from that contour (right)

order to identify the regions which will be processed in the further studies. The segmentation of the images to separate the nodule from the surrounding tissues is performed by means of a truncated median filter, a balloon algorithm and a dilation process. Due to the presence of Rayleigh distributed noise, which characterizes ultrasound images, the mode filter could be appropriate to denoise the images, since it eliminates the spurious negligible points. However, its performance depends strongly on the size of the window in which the filter is applied and, if it is not large enough, it may result in modeless regions or quite arbitrary values. That is why we have used the truncated median filter, which produces quite good results in a few iterations. In this filter, the median is calculated in each iteration and the further values are eliminated, so that the median and the mode approach. For a given pixel (x, y) , the process is as follows: let f_n be the histogram of the grayvalues in the $w \times h$ window from $(x - (w - 1)/2, y - (h - 1)/2)$ to $(x + (w - 1)/2, y + (h - 1)/2)$ (n ranges from 0 to 255), and let m be the median of such histogram, i.e. $\sum_{k=0}^{k=m-1} f_k < (w * h)/2$ and $\sum_{k=0}^{k=m} f_k \geq (w * h)/2$, those values which differ from m more than the minimum of m and $255 - m$ are

Fig. 10. Ultrasound image of a solid breast nodule (left), contour and calcifications extracted from that contour (right)

Fig. 11. Ultrasound image of a nodule (left), contour and center on the filtered image (right)

eliminated and the median is recalculated [7]. After a few iterations, the median can be considered as a good approximation of the mode.

From a seed into the nodule, which must be entered to the system by the user, a balloon algorithm allows filling the interesting area as connected intensity-similar pixels. The pixels which are connected to the already selected ones, whose intensity is similar to theirs and inside a certain interval are included into the selected region. If given two thresholds for intensity and difference, no more points can be incorporated, the thresholds are increased until no point is added in a given iteration or the added region is larger to the previous one, since the latter might mean that the background has been connected to the nodule.

Due to the difficulty that many of these images present, the user is allowed to correct the result of the automatic segmentation in case it does not fit the area covered by the nodule. Thus, adding and subtracting regions in the segmentation will produce a more reliable delimitation of the nodule to proceed to its analysis. Fig. 11 shows an example of the ultrasound image of a nodule (left), the filtered image, the contour and the center of the selected region (right).

3.2 Intensity-Related Features

In this section, we consider those factors which refer to the graylevels of the image, which represent the echo produced at each point when the ultrasound reaches it. These are the echogenicity of the nodule, the presence of acoustic shadow under the nodule, the microcalcifications and the observation of a thin echogenic capsule around the nodule.

Using the binary segmented image as a mask, we calculate the mean intensity of the region covered by the nodule. This is its mean echogenicity and, similarly, a fat region is selected by the user to extract its echogenicity and compare them. This comparison will help determining whether the nodule is hypo or hyperechogenic.

To determine whether the nodule is producing acoustic shadowing, we compare the region under the nodule and the region at the same level which is not covered by the nodule. As done before, we calculate the mean intensity (echogenicity) of both regions. The comparison of both mean intensities allows determining whether the nodule is absorbing the ultrasound or not.

By using the structure tensor method, we have estimated the magnitude of the gradient in every point inside the nodule. Those points where the intensity and the magnitude of the gradient is quite high have been selected as calcifications (see Fig. 10). In order to estimate the magnitude of the gradient, we first calculate an initial estimation for every point using the following mask for the horizontal component and its transpose for the vertical component:

$$u_x = \frac{1}{4h} \begin{pmatrix} -(2-\sqrt{2}) & 0 & (2-\sqrt{2}) \\ -2(\sqrt{2}-1) & 0 & 2(\sqrt{2}-1) \\ -(2-\sqrt{2}) & 0 & (2-\sqrt{2}) \end{pmatrix}. \quad (1)$$

For every point, we select an area around it and build the following matrix from the estimations of the gradient (x_n, y_n) in those points:

$$\begin{pmatrix} \sum_{i=0}^N y_i^2 & -\sum_{i=0}^N x_i y_i \\ -\sum_{i=0}^N x_i y_i & \sum_{i=0}^N x_i^2 \end{pmatrix}. \quad (2)$$

The eigenvector associated to the minimum eigenvalue is the estimation of the orientation of the gradient, and the maximum eigenvalue is the square of the norm of the gradient estimation.

The capsule of the nodule is extracted by eroding the selected region and analyzing the eroded points. The echogenicity of the capsule is measured, as the previous ones, from the mean intensity of the region.

3.3 Shape-Related Features

This section deals with those factors which refer to the shape of the nodule. The proportion of the width and the height of the nodule, the presence of angular

margins, the ramifications which may appear, the number and size of lobulations and the ellipsoid shape are considered as benign or malignant factors.

On the binary segmented image, we calculate the mean width and the mean height of the nodule and the quotient of both measures indicates its disposition. Besides, those points whose vertical distance to the center is larger than the mean width indicate the areas where the nodule is growing vertically. When studying whether the nodule has ellipsoid shape or not, we extract the ellipsoid for which the distance from the points on the contour is minimum. This yields the one which best represents the set of contour points (see Fig. 4). When the mean distance is low enough, the nodule has a clearly ellipsoid-like shape. On the other hand, the higher the distance, the more dissimilar the nodule and the ellipsoid are.

The usual techniques to estimate the ellipse location in an image are based on the Hough transform or the principal axis estimation [8][9]. We propose an algorithm to estimate, in a very accurate way, the ellipse location in an image by minimizing the mean distance from a set of points to the ellipse. This minimization criterion has a more physical meaning and provides a very accurate estimation.

An ellipse depends on 5 parameters $\Theta = (x_0, y_0, a, b, \theta)$, where (x_0, y_0) is the center, (a, b) are the sizes of the principal axes and θ is the orientation. We parametrize an ellipse in the following way:

$$e_{\Theta}(t) = \begin{pmatrix} x_0 + \cos(\theta)a \cos(t) + \sin(\theta)b \sin(t) \\ y_0 - \sin(\theta)a \cos(t) + \cos(\theta)b \sin(t) \end{pmatrix} \quad t \in [0, 2\pi] . \quad (3)$$

In the following lemma, we compute the distance from a point to an ellipse:

Lemma 1. *Let $(x, y) \in \mathbb{R}^2$, and let $e_{\Theta}(t)$ be an ellipse. The distance from the point (x, y) to the ellipse is denoted by $d((x, y), e_{\Theta}(\cdot))$. Such distance is attained in a point $t_0 \in [0, 2\pi]$. If $z = \cos^2(t_0)$ then z is a root of the polynomial*

$$l^2 z^4 + 2mlz^3 + (k + 2ln + m^2)z^2 + (2mn - k)z + n^2 = 0 . \quad (4)$$

where

$$\begin{aligned} \tilde{x} &= \cos(\theta)(x - x_0) - \sin(\theta)(y - y_0) \\ \tilde{y} &= \sin(\theta)(x - x_0) + \cos(\theta)(y - y_0) \\ l &= -(b^2 - a^2)^2, \quad m = (b^2 - a^2)^2 + a^2\tilde{x}^2 - b^2\tilde{y}^2, \quad k = 4\tilde{x}^2\tilde{y}^2a^2b^2, \quad n = -\tilde{x}^2a^2 \end{aligned}$$

Proof: A straightforward calculation.

Given a set of points $X = \{(x_i, y_i)\}_{i=1, \dots, N}$, we define the mean distance from an ellipse to the set of points X as

$$d(X, e_{\Theta}(\cdot)) = \frac{1}{N} \sum_{i=1, \dots, N} d((x_i, y_i), e_{\Theta}(\cdot)) . \quad (5)$$

Next, we minimize the distance from X to the ellipse with respect to the parameters of the ellipse Θ . We propose a gradient descent method to perform the

minimization procedure. We start with an initial approximation for the ellipse parameters which could be provided by the Hough transform or another simpler method. Then, we iterate the scheme:

$$\Theta^{k+1} = \Theta^k - \lambda \nabla_{\Theta} d(X, e_{\Theta^k}(.)) . \quad (6)$$

The step λ is adapted in each iteration using the following criterion: We initialize $\lambda = \lambda_0$, we compute Θ^{k+1} from Θ^k using (6). If $d(X, e_{\Theta^{k+1}}(.)) < d(X, e_{\Theta^k}(.))$, we update $\lambda = 10\lambda$. If $d(X, e_{\Theta^{k+1}}(.)) > d(X, e_{\Theta^k}(.))$, we update $\lambda = 0.1\lambda$ and we recompute Θ^{k+1} . We stop the iterative scheme when $\Theta^{k+1} - \Theta^k$ is small enough, or when we cannot reduce $d(X, e_{\Theta^k}(.))$ after a number of attempts. The distance is divided by the square root of the area of the nodule to normalize it. If the nodule has not ellipsoid shape, we must determine if it has two or three gentle lobulations. We proceed as in the previous case, but instead of searching for an ellipsoid which fits the whole contour, we search for large lobulations which fit a large region of the contour each, which together cover the whole contour, whose axes do not differ strongly in their lengths, and whose centers are clearly separated (see Fig.5).

To analyze whether the nodule presents ramifications, we locate those points whose distance to the ellipsoid which best fits the nodule is large. Since the ellipsoid covers the most representative part of the nodule, when it has ramifications, they appear as branches projecting out from this ellipsoid. The number and dimensions of these ramifications is strongly considered to characterize the nodule.

In order to prevent the ramifications from influencing the position and dimensions of the main ellipse, an iterative scheme has been used in which the points which are very far from the ellipse are eliminated and the ellipse is recalculated. After a few iterations, the ellipse which is extracted is much more representative of the central region and the ramifications are more clearly identified (see Fig. 6).

We can locate angular margins by searching for pseudo-straight lines on the contour of the nodule. In order to adjust a set of N points to a straight line, we proceed as follows:

Let (u, v) be a point, and let $r = x + ay + b$ be a line, the distance from (u, v) to $x + ay + b$ is:

$$d(m, r) = \frac{|u + av + b|}{\sqrt{1 + a^2}} . \quad (7)$$

If we minimize with respect to a and b , we obtain the values which best extract the supporting line for a set of planar points.

When a point joins two straight lines with different orientations, an angle is signaled. In order to select those angles which are significant for the study, the lines must fit the contour, i.e. the mean distance from the points on the contour to the line must be low, they must be long enough in order to neglect small variations in the orientation of the contour, and the difference in the orientation must be less than $\pi/2$, i.e. they form an acute angle (see Fig. 7). For every

candidate to be a pseudo-corner, the line which adjusts the points before it in the contour and the line which adjusts the points after it, considering the contour as a sequence, must be extracted and compared.

Besides angular margins, we may find microlobulations. For this feature, a similar technique as the one used when extracting the general ellipsoid is applied. However, in this case, we search for segments of the contour which can be approximated by a part of an ellipse and whose size and axes are small. In order to avoid the duplication of the lobulations by extracting overlapping ellipses, only those whose centers are clearly different are selected (see Fig. 8).

To locate the areas where spiculation appears, we extract the orientation of a window around every contour point. As done with the calcifications, the structure tensor method has been used, though, in this case, not only the magnitude of the gradient, but also its orientation is significant. When the orientation in that region is quite dissimilar to the one of the contour in that point, it is marked as a spiculation zone (see Fig. 9). Non-spiculated nodules present a clearly defined contour along which the orientation varies softly. Similarly as done when we calculated the magnitude of the gradient for the localization of the calcifications, we now extract the magnitude and the orientation.

We have tested the measurements extracted for the different criteria by considering ultrasound images of 40 solid breast nodules. To estimate the relevance of the information provided by each factor in the diagnosis, we have calculated the area under the ROC curve for each one of them. This curve relates the sensibility and the specificity of a diagnostic criterion, and the closer to 1 the area is, the more powerful the criterion is. The best results were obtained for microlobulations (0.854), angular margins (0.849), ellipsoid shape (0.794) and ramifications (0.789).

4 Conclusion

In this paper, we have presented a new approach in the field of breast cancer early detection. We have dealt with a very difficult type of images, those generated by ultrasound devices, which present a dense and intense kind of noise and whose interpretation is quite difficult, even for a human observer.

The definition of a series of objective and reliable criteria for the discrimination between benign and malignant solid breast nodules and their relation to visual characteristics of a region have made it possible to apply those techniques used in shape and texture analysis to the description of those nodules.

A wide range of techniques, such as truncated median, seed segmentation, shape adjustment, ellipse location or structure tensor, have allowed reaching very satisfactory results in terms of quantitative and qualitative description of the criteria that the physicians take into account when diagnosing a nodule.

The possibility of providing objective numerical measurements of the presence of the diagnosis criteria represents a remarkable progress in the classification of the nodules.

These results emphasize the importance of the introduction of computer vision techniques in the processing of medical images, not to substitute the role of the physicians, whose skills can only be imitated in a hard and limited way, but to aid the decision making process.

References

1. Kuo, W.J., Chang, R.F., Moon, W.K., Lee, C.C., Chen, D.R.: Computer-Aided Diagnosis of Breast Tumors with Different US Systems. *Acad Radiol* **9** (2002) 793-799
2. Kaufhold, J., Chan, R., Karl, W.C., Castanon, D.A.: Ultrasound Tissue Analysis and Characterization. *Battlefield Biomedical Technologies*, H.H. Pien editor, *Proc. SPIE* **3712** (1999) 73-83
3. Chen D.R., Chang, R.F., Juang, Y.L.: Computer-Aided Diagnosis Applied to US of Solid Breast Nodules by Using Neural Networks. *Radiology* **213** (1999) 407-412
4. Cheng, C.M., Chou, Y.H., Han, K.C., Hung, G.S., Tiu, C.M., Chiou, H.J., Chiou, S.Y.: Breast Lesions on Sonograms: Computer-Aided Diagnosis with Nearly Setting-Independent Features and Artificial Neural Networks. *Radiology* **226** (2003) 504-514
5. Stavros, A.T., Thickman, D., Rapp, C.L., Dennis, M.A., Parker, S.H., Sisney, G.A.: Solid Breast Nodules: Use of Sonography to Distinguish between Benign and Malignant Nodules. *Radiology* **196** (1995) 123-134
6. Sonka, M., Hlavac, V., Boyle, R.: *Image Processing, Analysis, and Machine Vision*. PWS-ITP (1999)
7. Nixon, M.S., Aguado, A.S.: *Feature Extraction and Image Processing*. Oxford Newnes (2002)
8. Ahn, S.J., Rauh, W., Warnecke, H.J. Least-Squares Orthogonal Distances Fitting of Circle, Sphere, Ellipse, Hyperbola, and Parabola. *Pattern Recognition*, Elsevier **34** (2001) 2283-2303
9. Halír, R., Flusser, J. Numerically Stable Direct Least Squares Fitting of Ellipses. In *Proc. of WSCG 98* (1998) 125-132